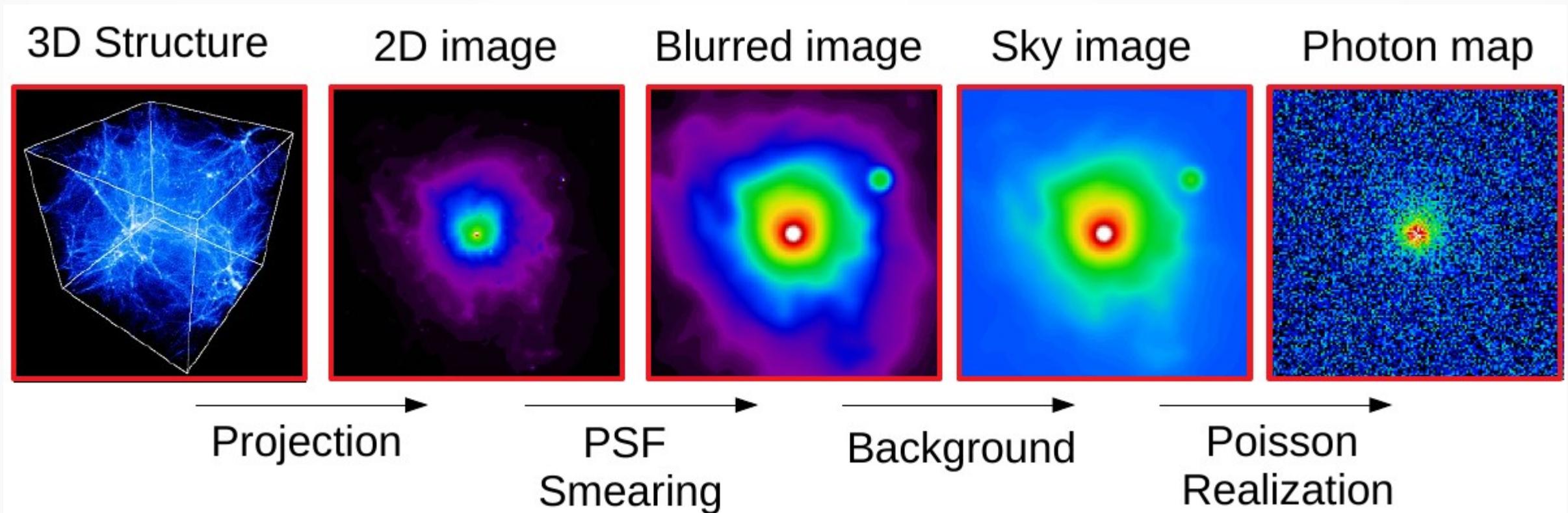


# Bayesian analysis of galaxy cluster properties with *pyproffit* and *hydromass*

**Dominique Eckert, Stefano Ettori**

# Deconvolution amplifies noise

- Observed galaxy cluster profiles are noisy realizations of *projected* and *PSF-convolved* physical quantities

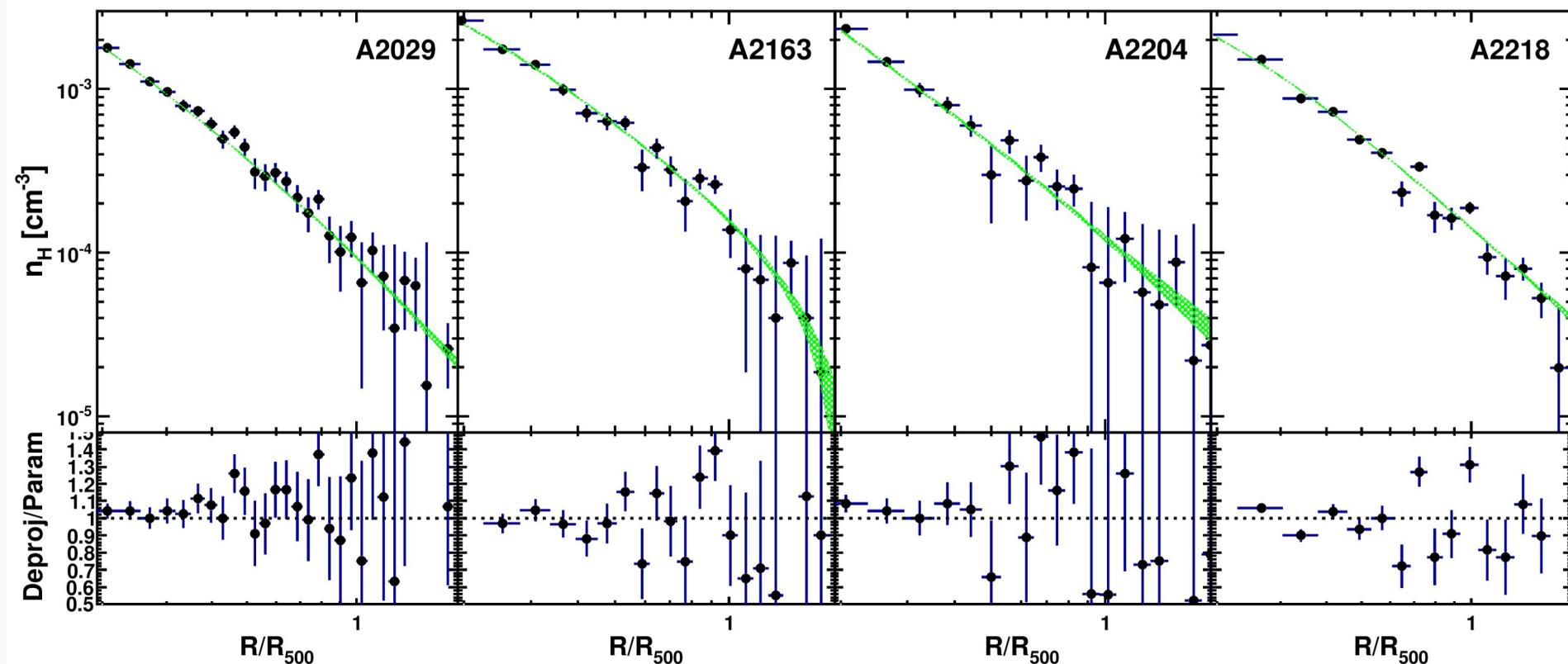


- The convolution kernel smooths fluctuations, thus deconvolution has the opposite effect

# “Traditional” approaches

**Parametric form:** Only as good as what the adopted function can reproduce

**Direct inversion:** Amplifies noise, depends on the chosen binning, can lead to unphysical solutions



# Decomposition on a basis of functions

- **Multiscale approach:** decompose the observed profile onto a basis of functions which can be individually deprojected/deconvolved

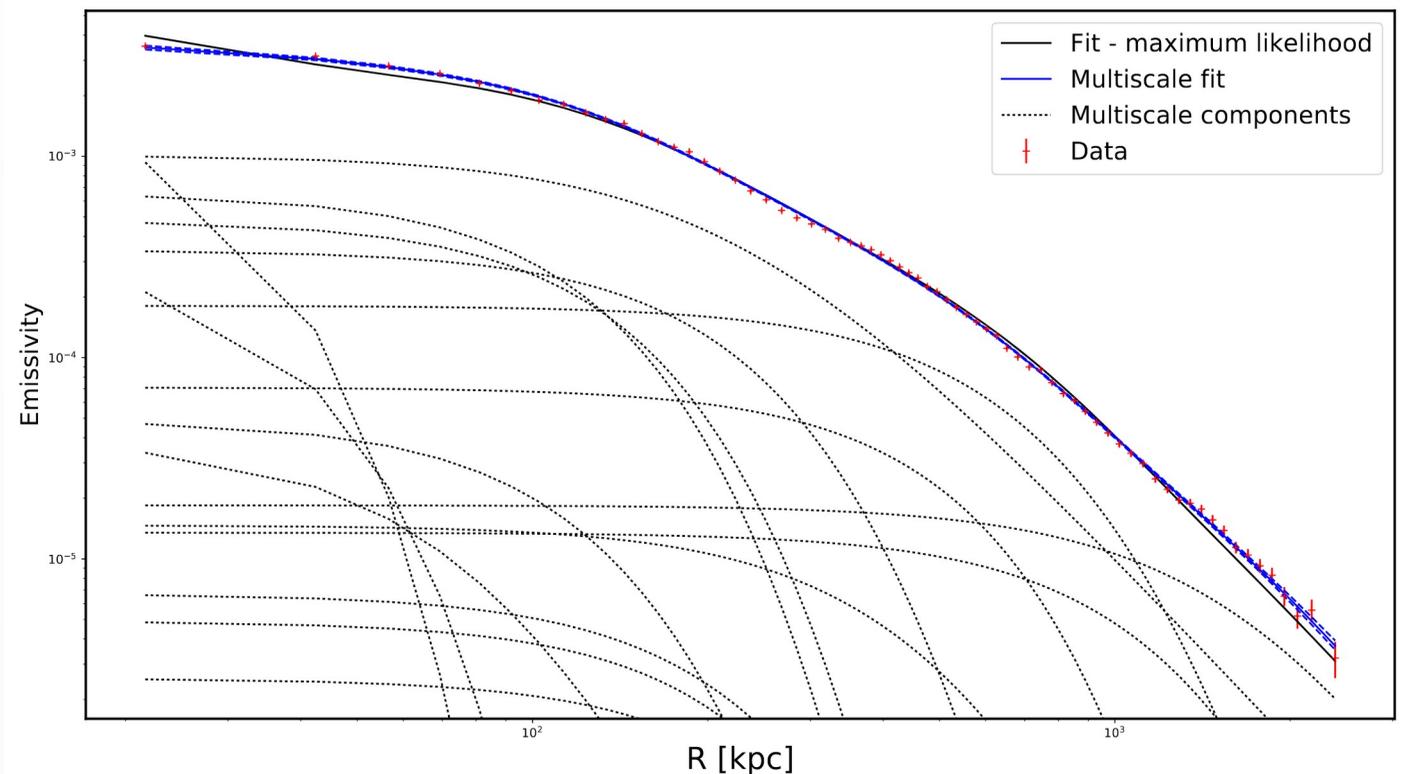
$$\epsilon_{3D}(r) = \sum N_i \Phi_i(r)$$

$$S_X(\omega) = \int_{-\infty}^{\infty} \epsilon_{3D}(r) dz \quad \omega = \sqrt{x^2 + y^2}$$
$$= \sum \alpha_i \phi_i(\omega)$$

The relations

$$\Phi_i \rightarrow \phi_i \quad N_i \rightarrow \alpha_i$$

can be computed once and for all

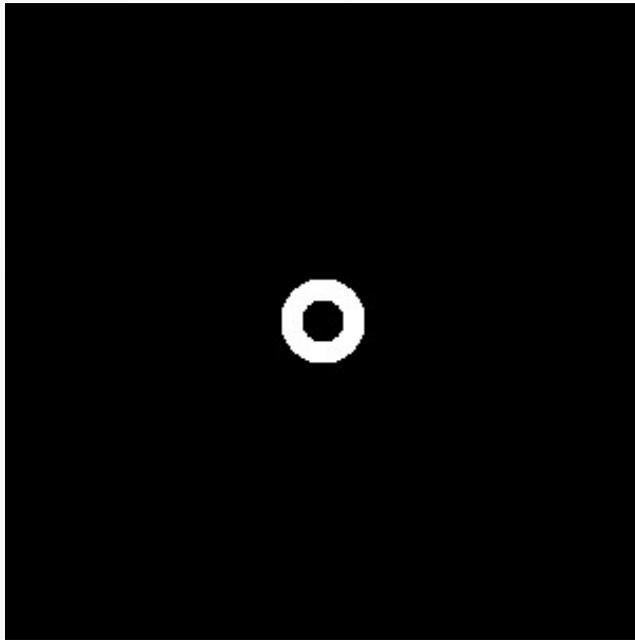


- **Optimization** performed with Hamiltonian Monte Carlo (PyMC3)

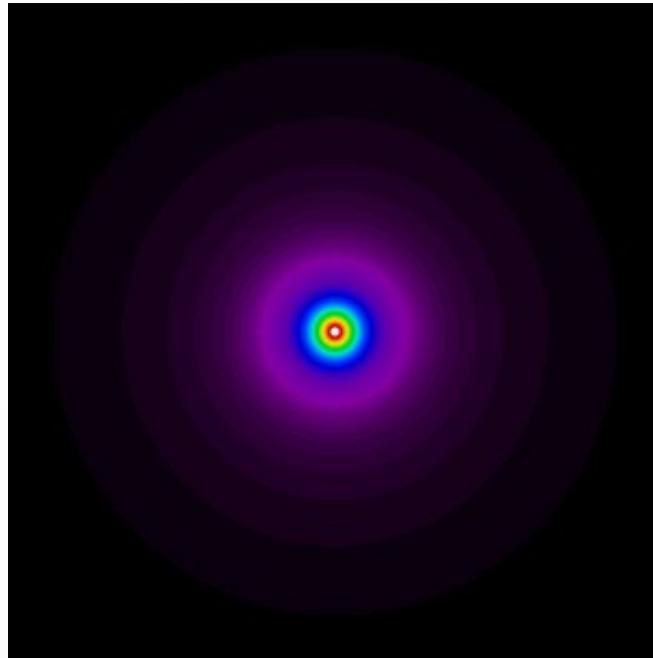
# PSF deconvolution

- To account for PSF smearing we create a PSF mixing matrix using FFT

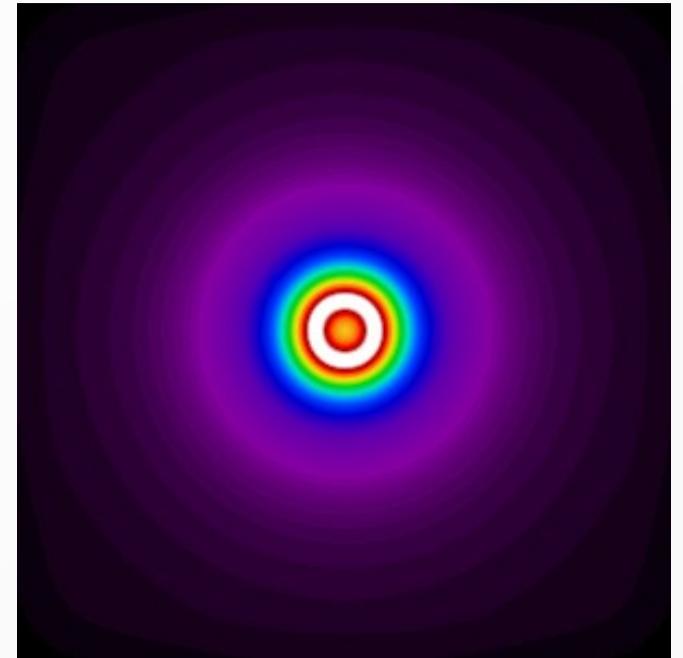
Annulus



Kernel



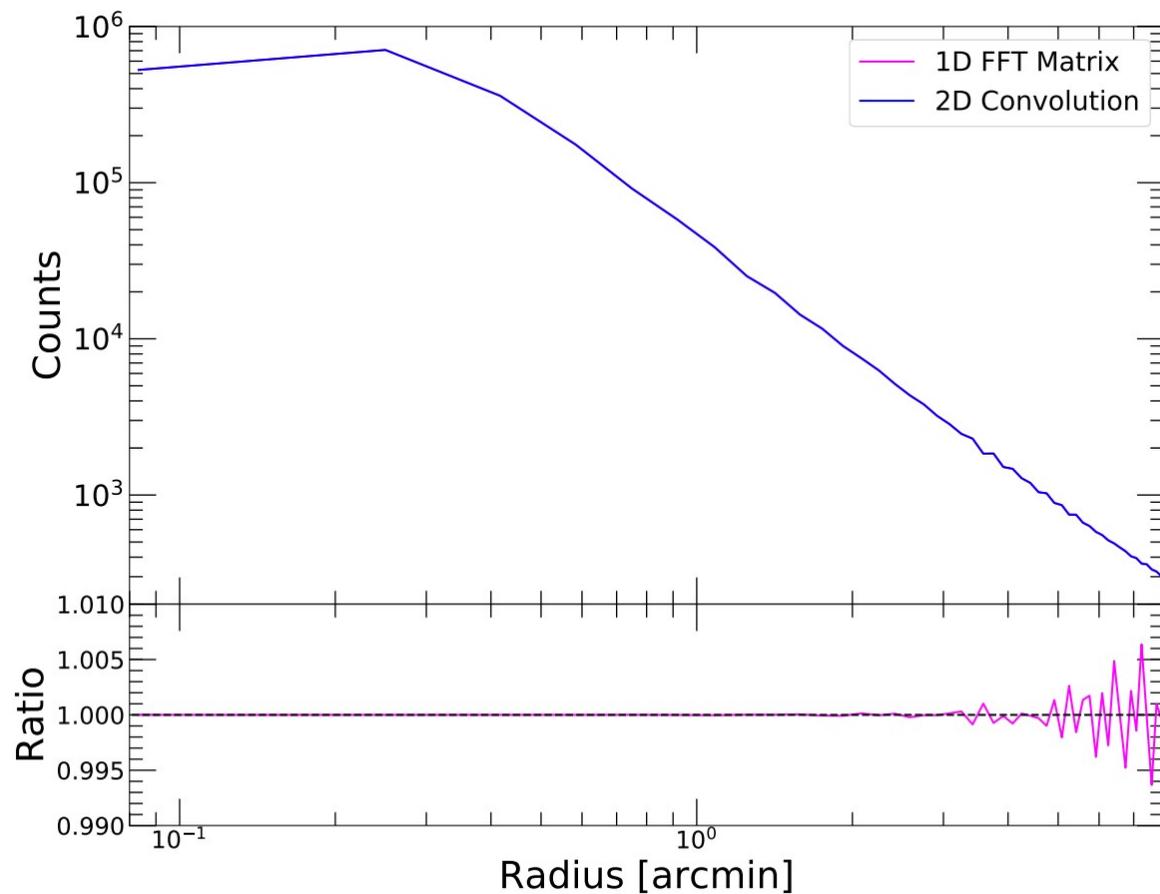
Convolved



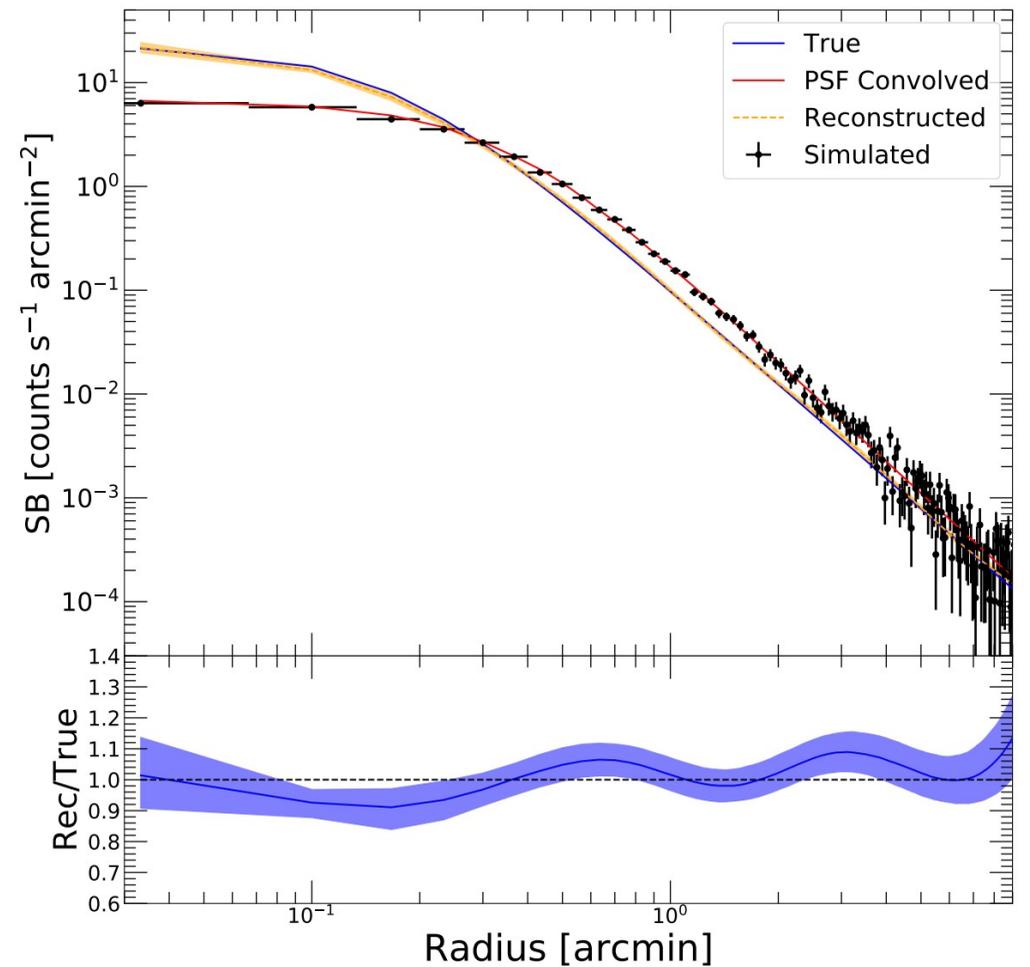
We count the fraction of photons being recorded annulus by annulus, and repeat the operation for each annulus

# PSF convolution: tests

Point source

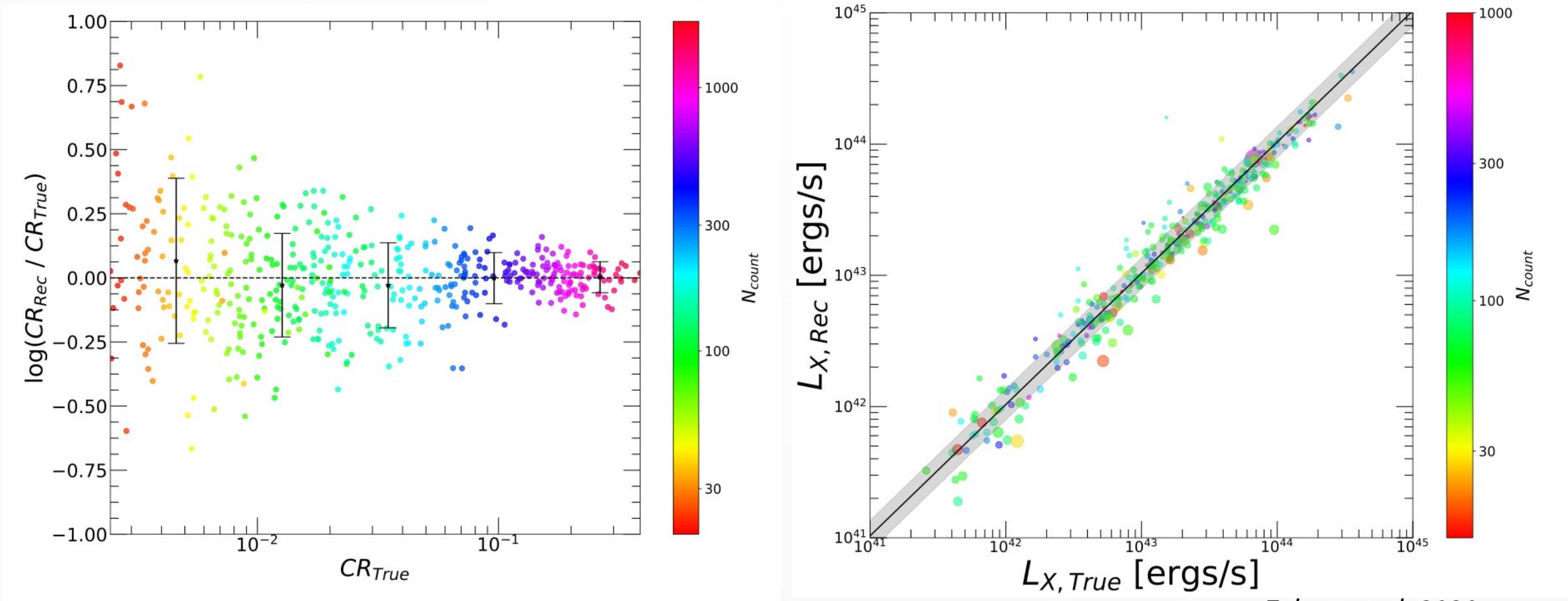


Beta model



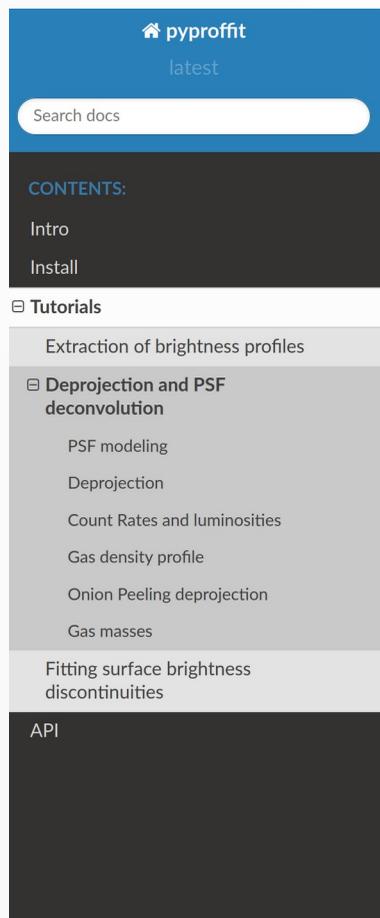
# Integrated quantities

- The code is able to determine accurate luminosities, including core-excised ones, even for sources detected with 30 counts



# Pyproffit: a Python package for surface brightness analysis

- The code is distributed in the public Python package *pyproffit*



The screenshot shows the Pyproffit documentation website. At the top, there is a blue header with the text 'pyproffit' and 'latest'. Below the header is a search bar labeled 'Search docs'. A 'CONTENTS:' section follows, listing 'Intro' and 'Install'. Underneath is a 'Tutorials' section with a dropdown arrow, containing a list of topics: 'Extraction of brightness profiles', 'Deprojection and PSF deconvolution' (with a dropdown arrow), 'PSF modeling', 'Deprojection', 'Count Rates and luminosities', 'Gas density profile', 'Onion Peeling deprojection', and 'Gas masses'. Below this is 'Fitting surface brightness discontinuities' and 'API'.

[Docs](#) » [Tutorials](#) » Example: Deprojection, gas density profiles and gas masses [Edit on GitHub](#)

## Example: Deprojection, gas density profiles and gas masses

This thread shows how to use *PyProffit* to extract gas density profiles, gas masses, integrated count rates and luminosities from imaging data. This code implements the method presented in Eckert et al. (2020) to apply deprojection and PSF deconvolution.

We start by loading the data and extracting a profile...

```
[1]: import numpy as np
import pyproffit
import matplotlib.pyplot as plt

[2]: import os

# Change this to the proper directory containing the test data
os.chdir('../validation/')

[3]: dat=pyproffit.Data(imglink='b_37.fits.gz',explink='expose_mask_37.fits.gz',
                        bglink='back_37.fits.gz')

WARNING: FITSFixedWarning: RADECSYS= 'FK5 ' / Equatorial system reference
the RADECSYS keyword is deprecated, use RADESYSa. [astropy.wcs.wcs]
```

Now we extract a profile in circular annuli from the surface brightness peak...

<https://pyproffit.readthedocs.io>

# Non-parametric log-normal mixture deprojection

- We suppose that the function of interest (temperature profile) can be described as a linear combination of a large number (P) of log-normal functions

$$T(r) = \sum_{i=1}^P N_i \frac{1}{\sqrt{2\pi\sigma_i^2}} \exp\left(\frac{-(\ln(r) - \ln(\mu_i))^2}{2\sigma_i^2}\right)$$

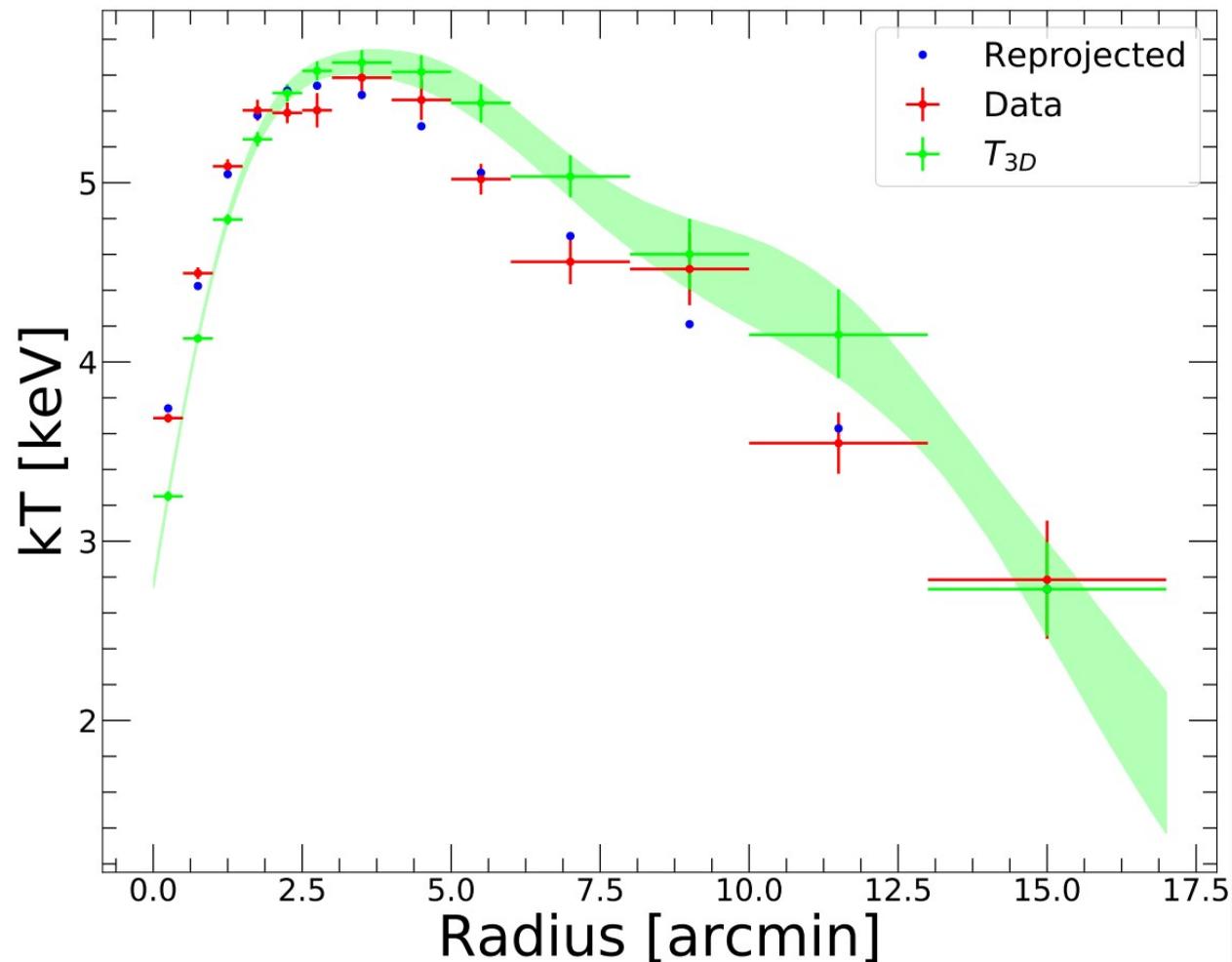
- For a basis of functions  $\{G_i\}$  characterized by predefined means  $\{\mu_i\}$  and standard deviations  $\{\sigma_i\}$ , the temperature profile can be determined by optimizing the normalizations  $\{N_i\}$ ,

$$\log L = -0.5 \sum_{j=1}^N \frac{(T_j - T_{model}(r_j))^2}{\sigma_{T,j}^2}$$

with  $T_{model}$  a function of  $T(r)$  given above.

# Non-parametric 3D temperature profile reconstruction

- Example: A1795



Red: 2D temperature data

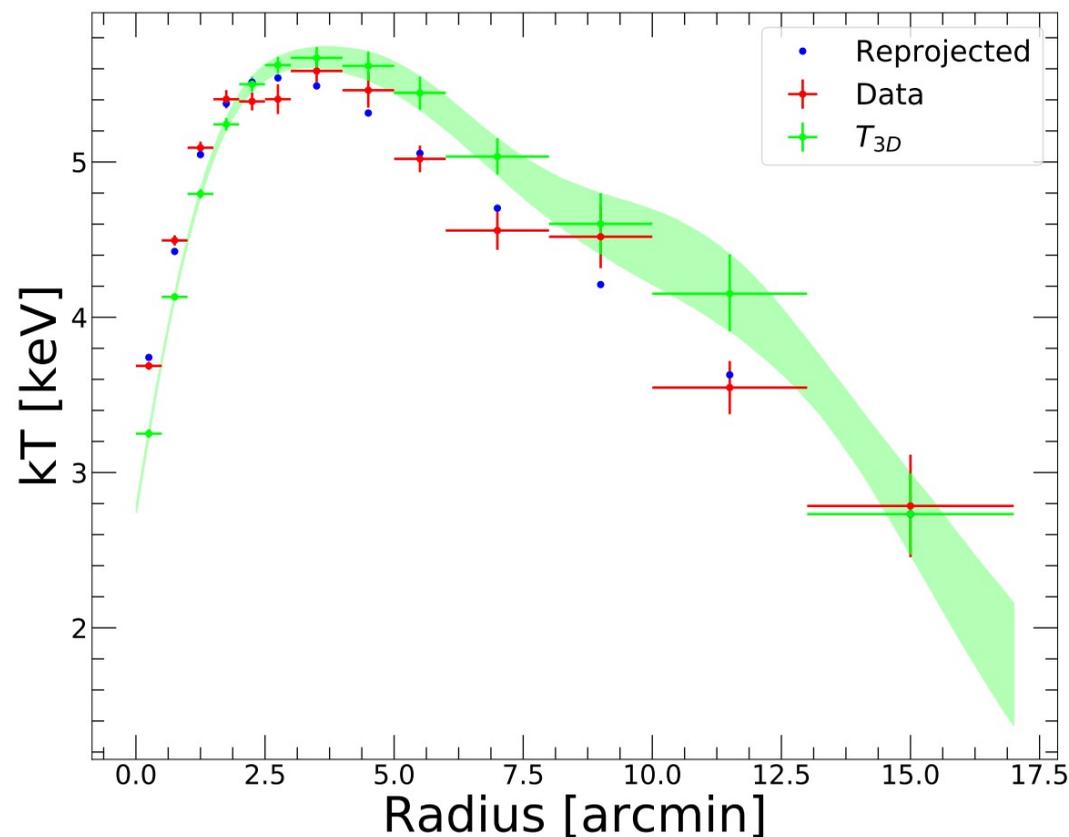
Green: 3D model obtained with PyMC3

Blue: Best-fit 3D model reprojected to compare with data

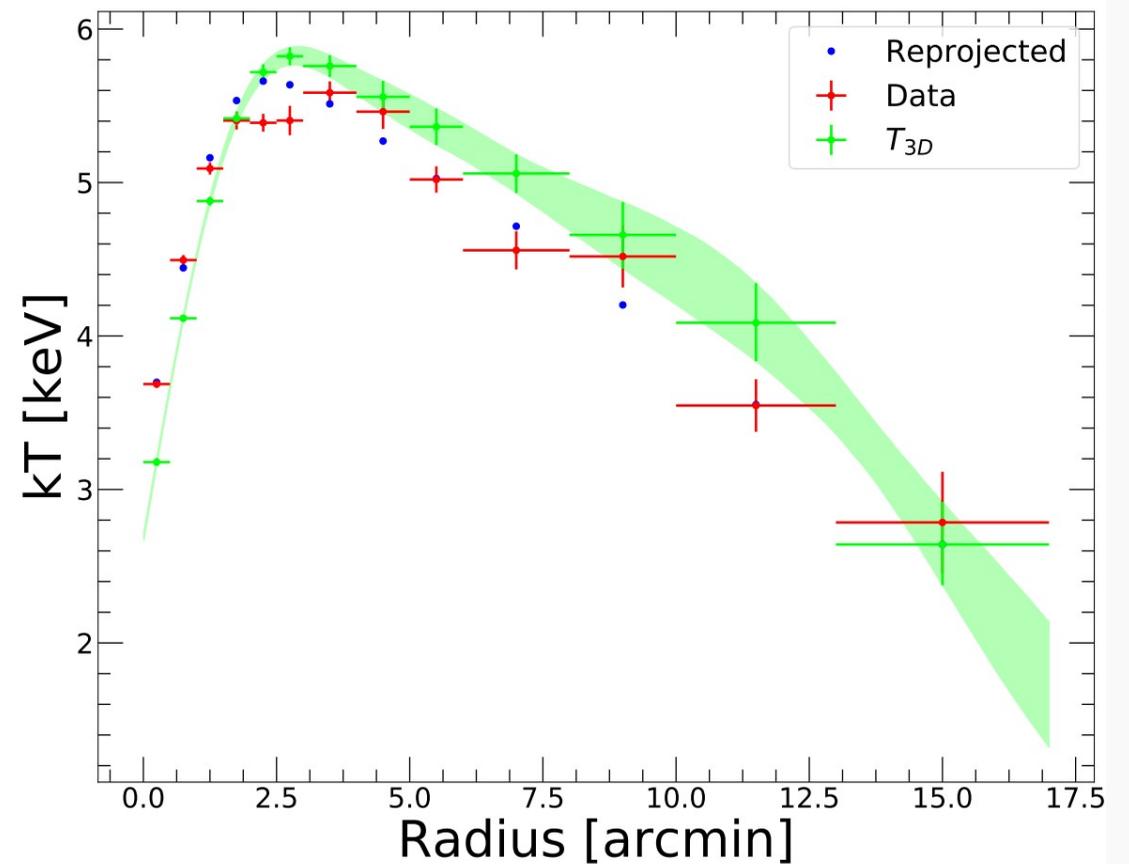
# PSF convolution of temperature profiles

- In this case the relation between  $T_{2D}$  and  $T_{3D}$  is the same as before, but with a matrix  $T = \text{PSF} \cdot V$

w/o PSF

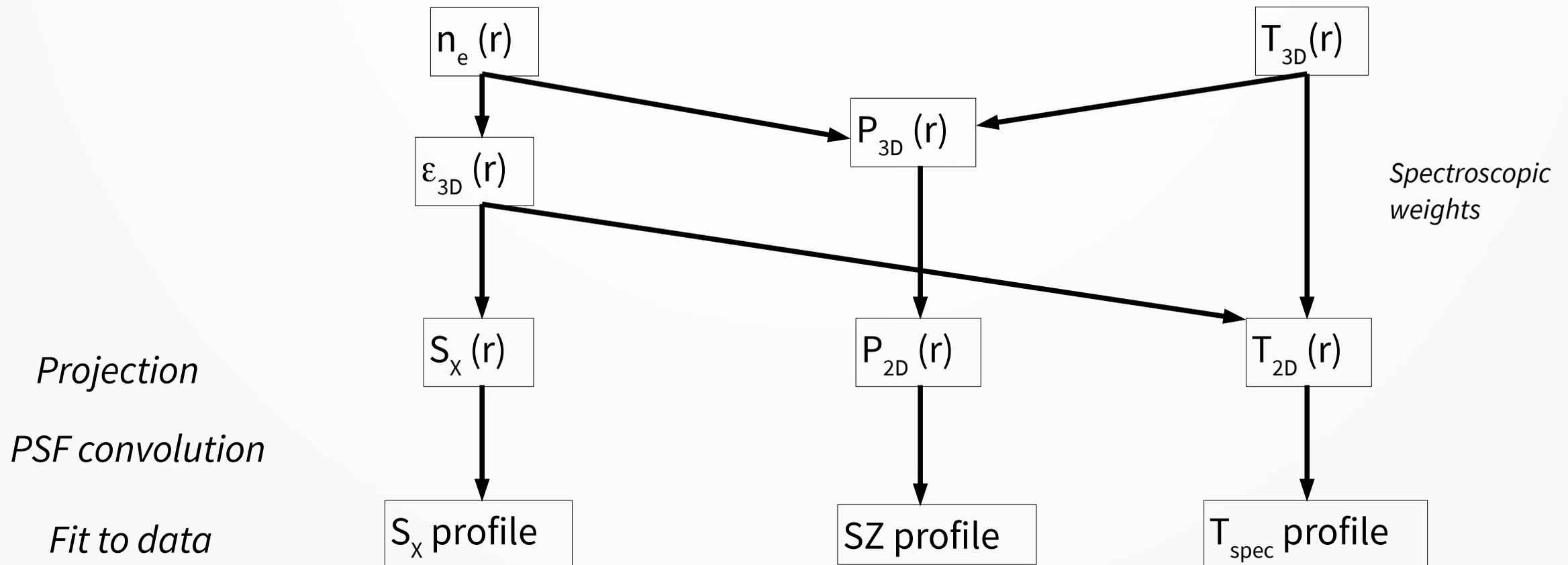


w PSF



# Hydrostatic mass reconstruction

- The multiscale density and temperature models can be optimized jointly



# Fitting a mass model

- If we choose to use a parametric mass model:

$$M(<r) = f(r, \theta)$$

- The “total” HSE pressure becomes

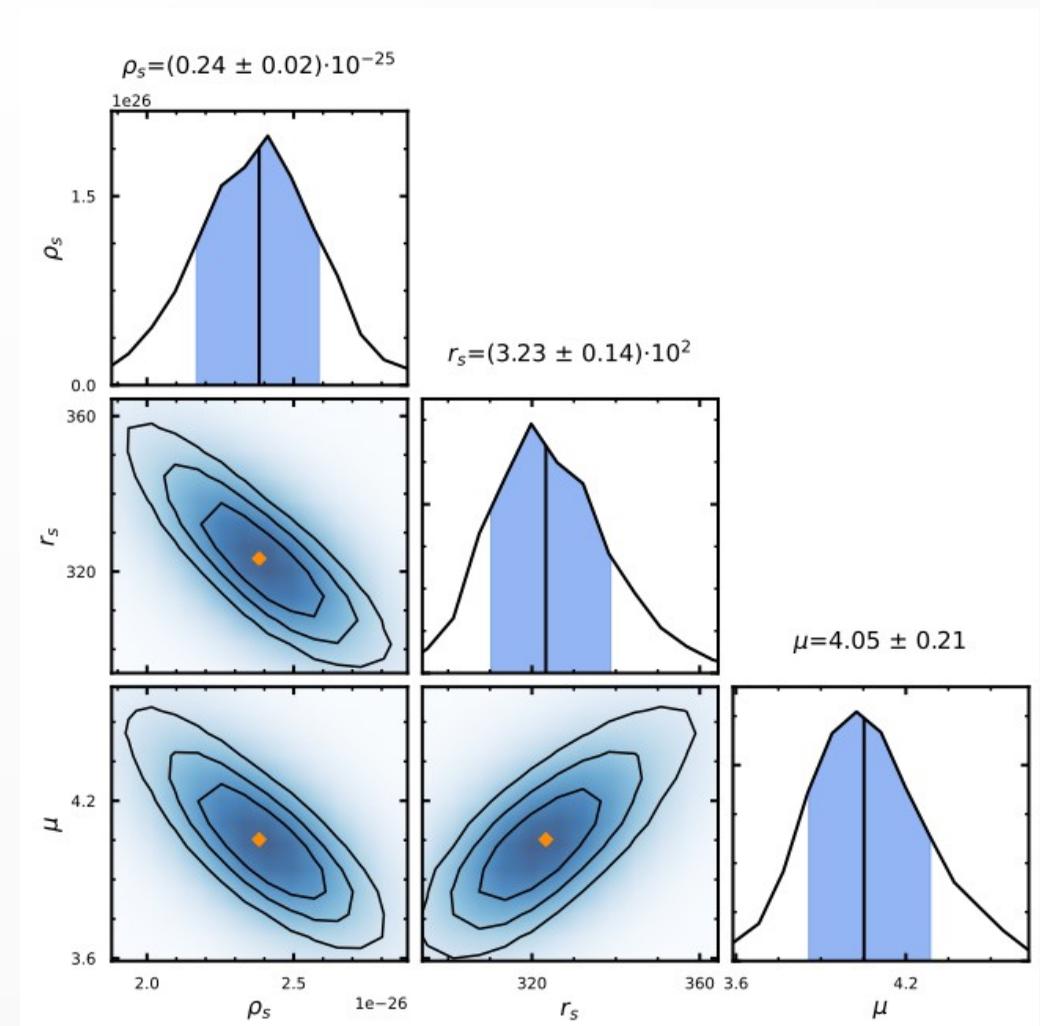
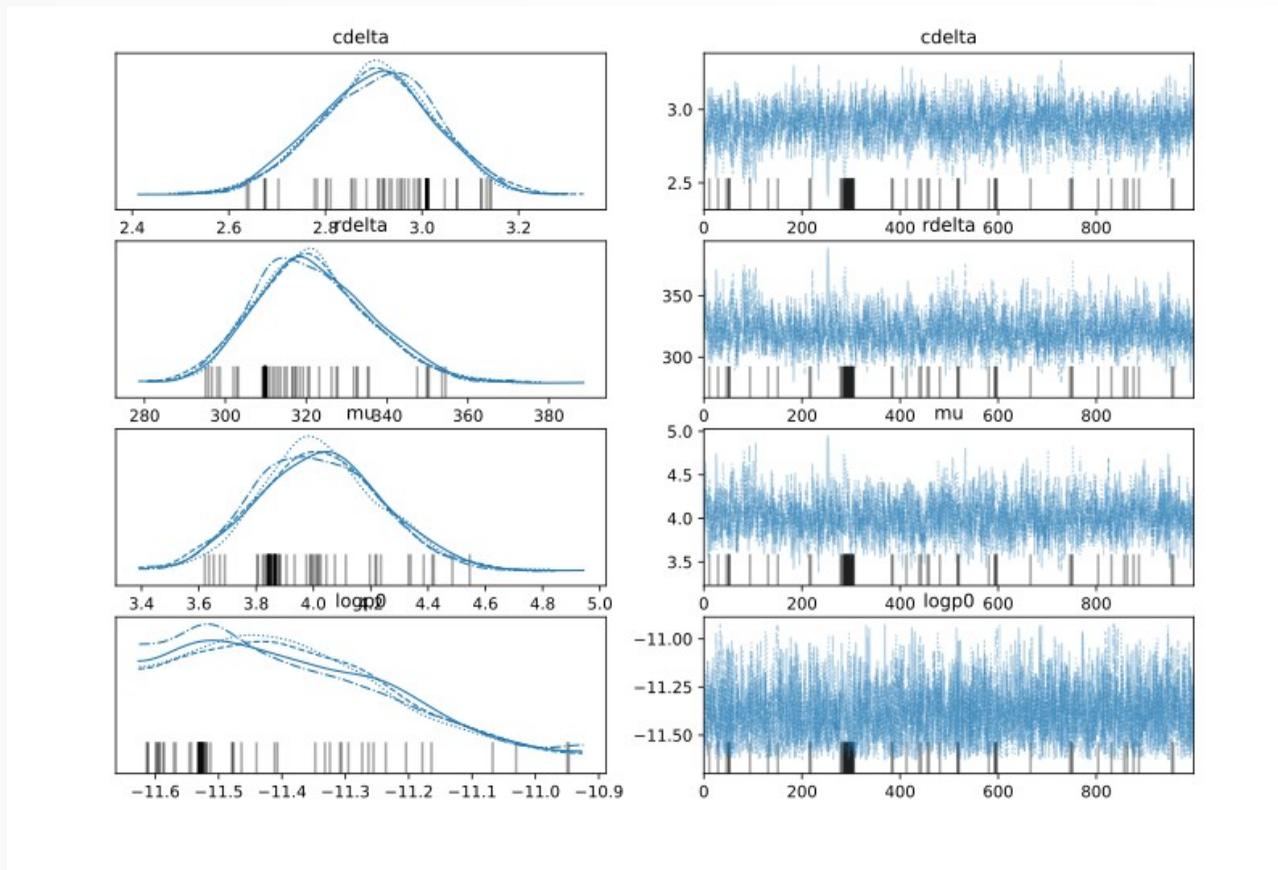
$$P(r, \theta) = P_0 + \int_r^{r_0} \frac{\rho_{gas} G f(r', \theta)}{r'^2} dr'$$

with  $r_0$  the outermost radius of the profile and  $P_0$  the pressure at  $r_0$

- At any point in the fitting process, multiscale parameters predict  $\rho_{gas}$  such that with the mass model we can predict  $P(r, \theta)$
- Priors on the model parameters  $\theta$  can be easily set in the code

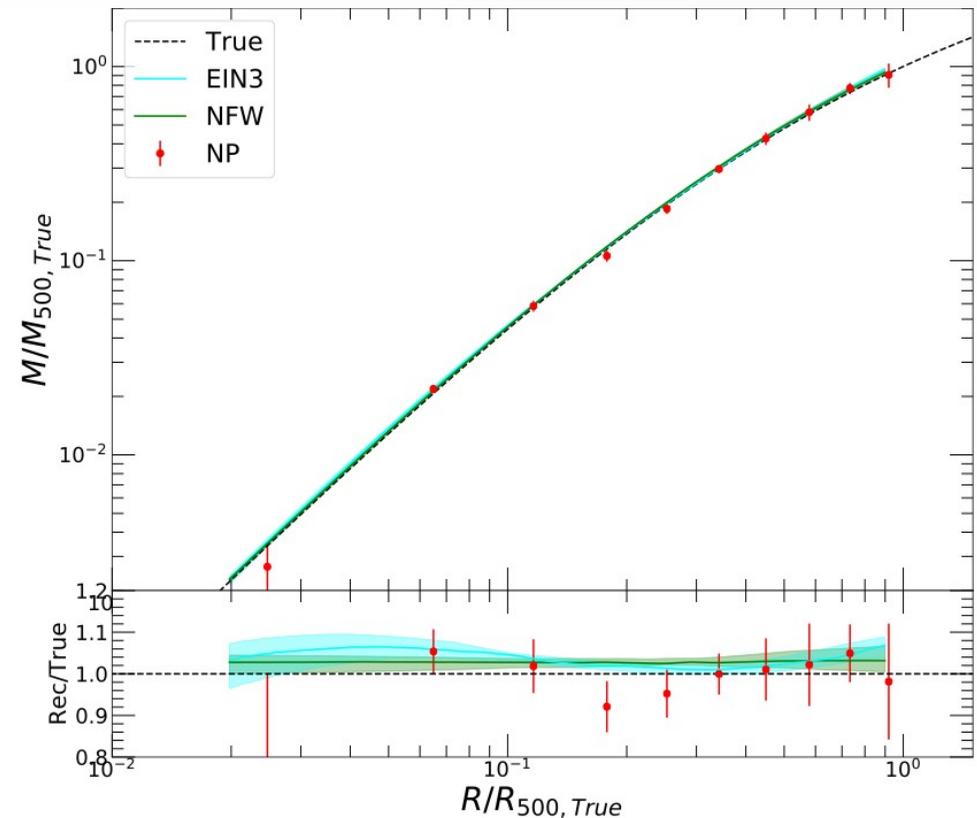
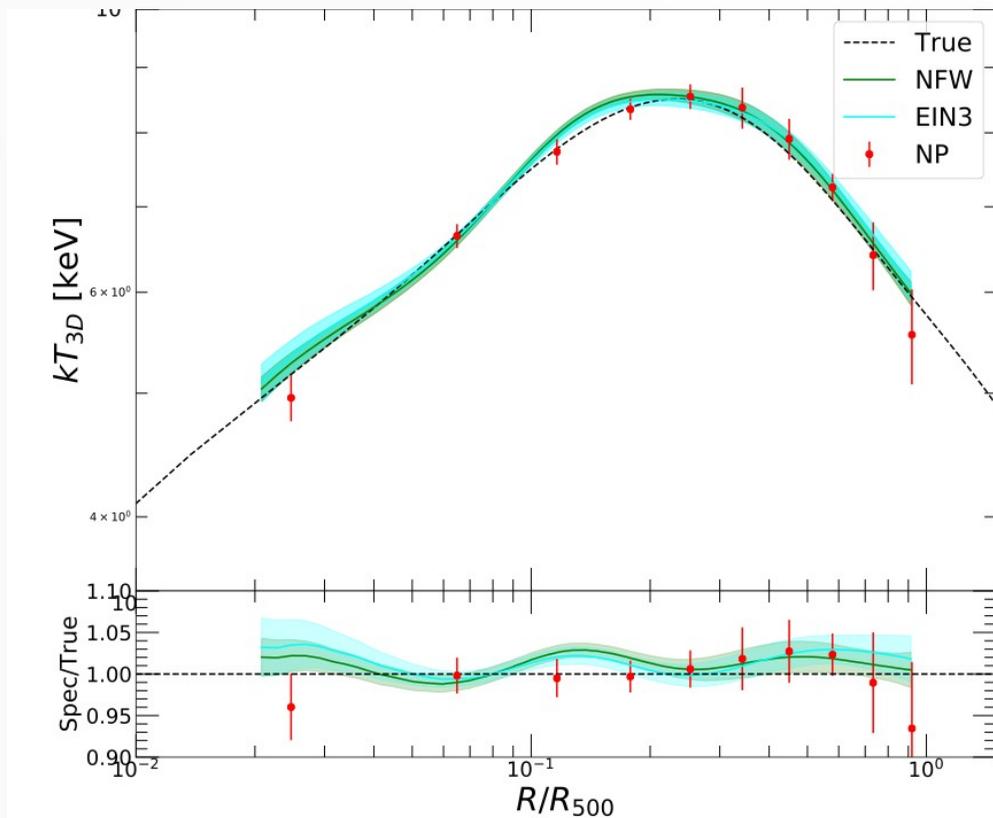
# Posterior parameter distributions

- Example posterior distributions for the Einasto fit



# Tests on mock data

- We created mock XMM observations of a fiducial NFW cluster, including projection, PSF convolution, energy redistribution etc.

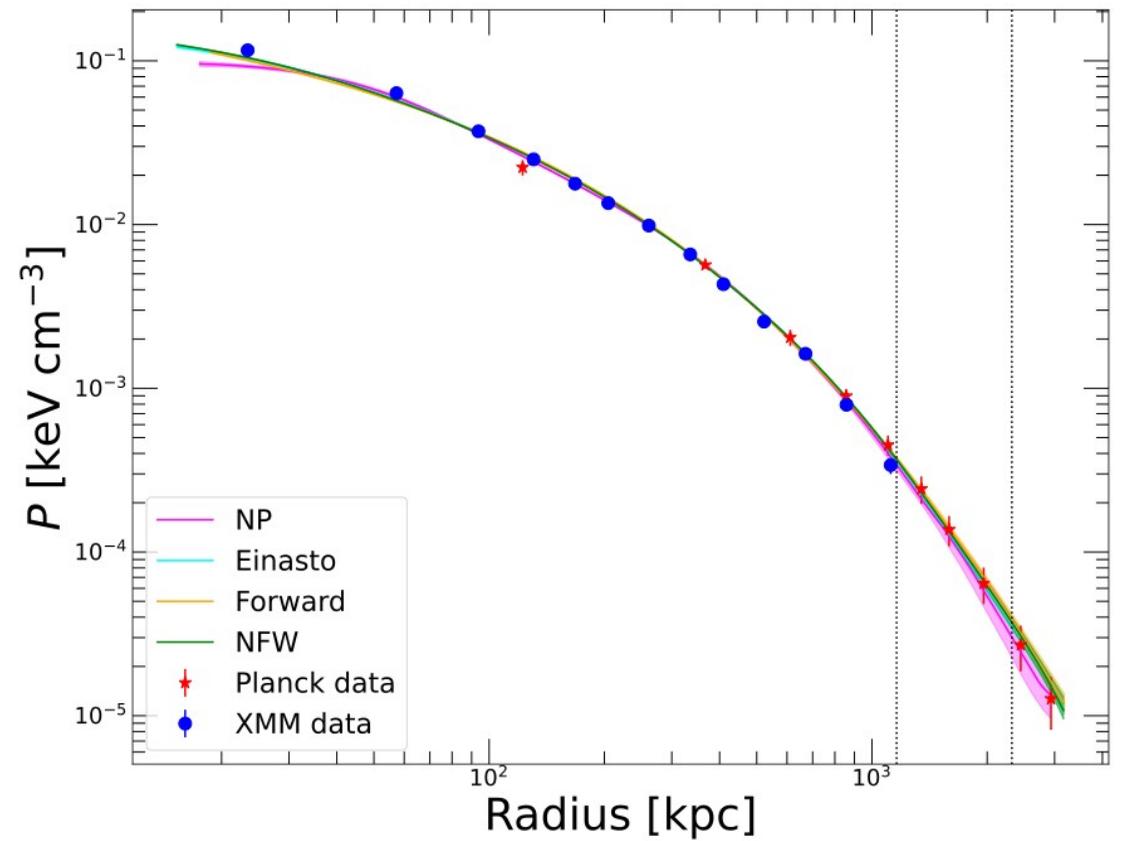
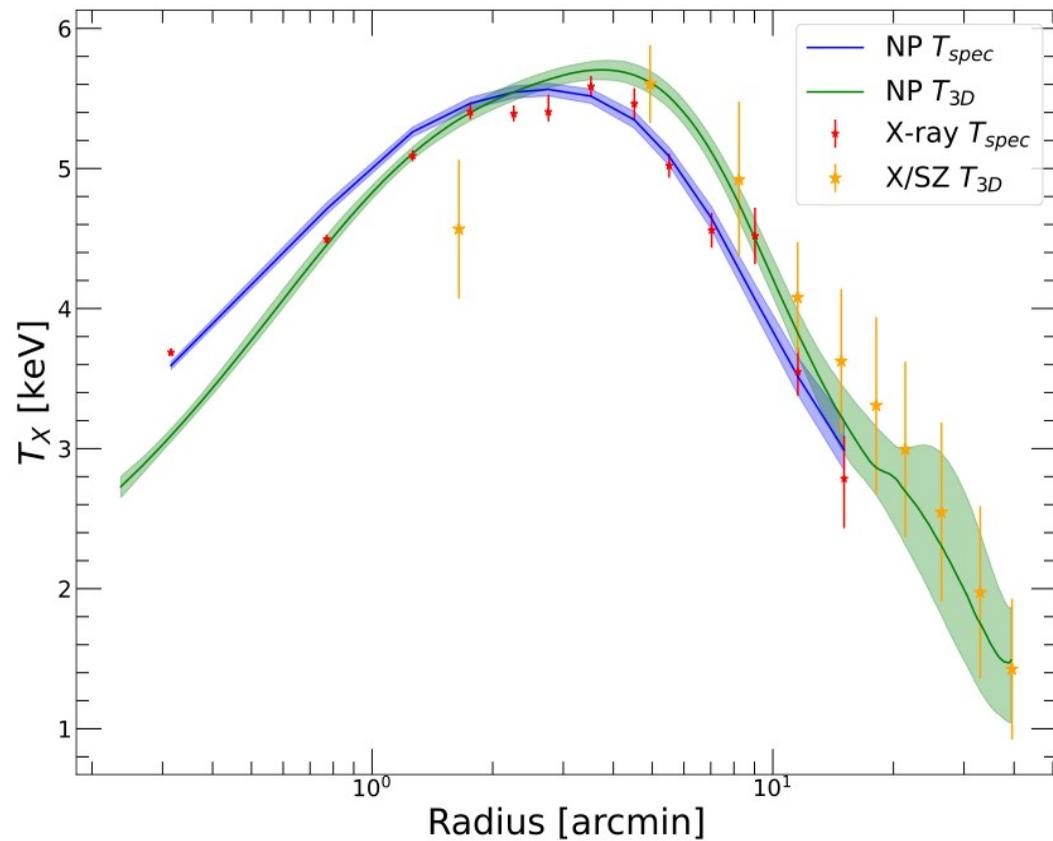


- Our code recovers the true profile with  $<3\%$  accuracy

*Eckert et al. 2022a*

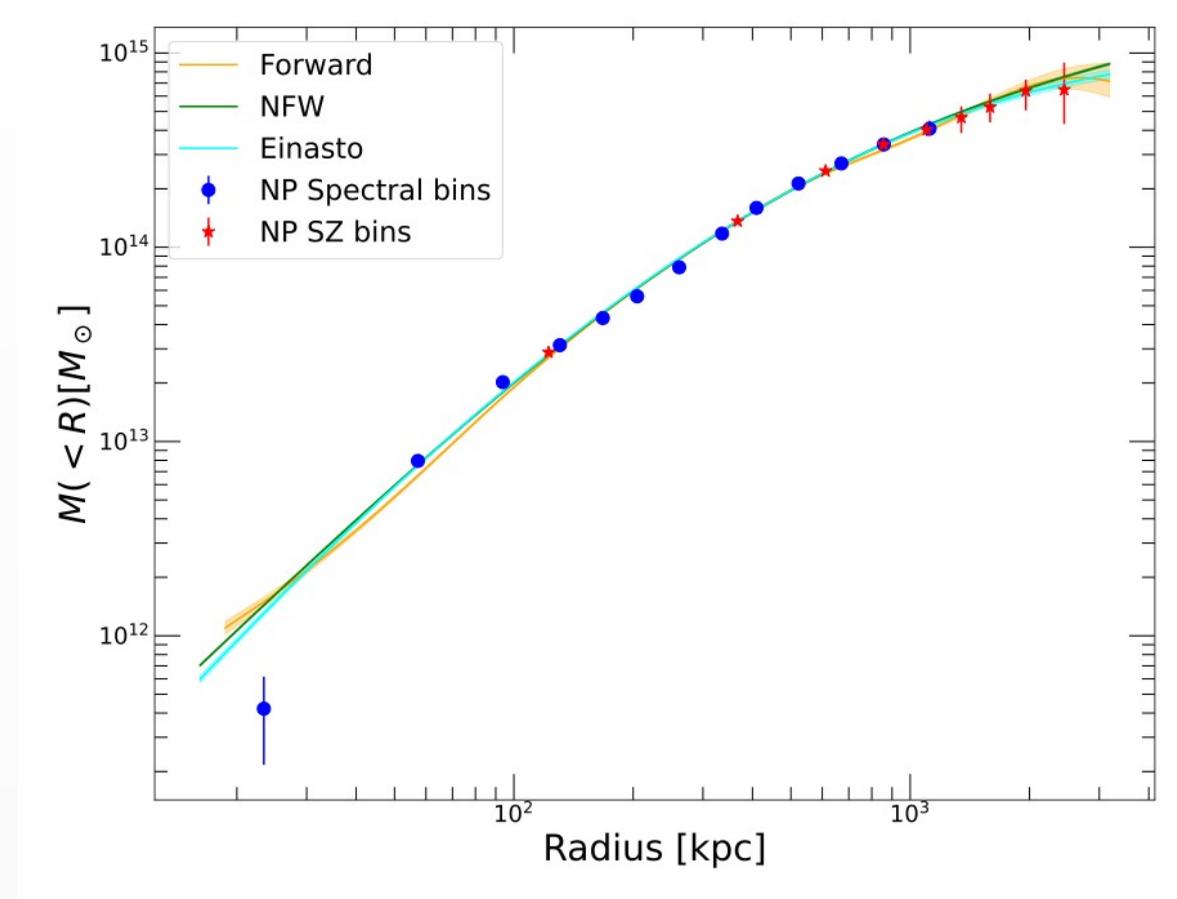
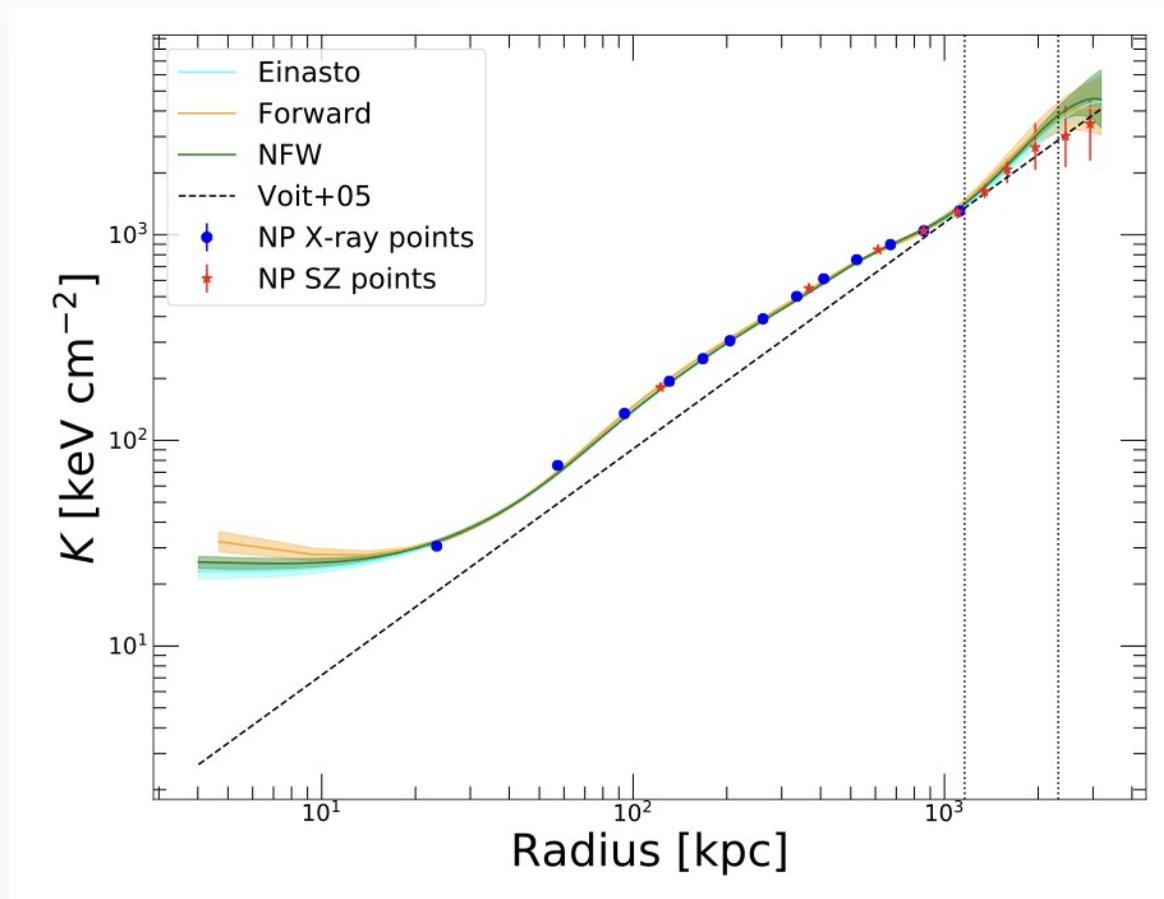
# Example: application to A1795

- Joint XMM + Planck reconstruction of the 3D cluster properties



# Application to A1795

- Derived thermodynamic and mass profiles



# Summary

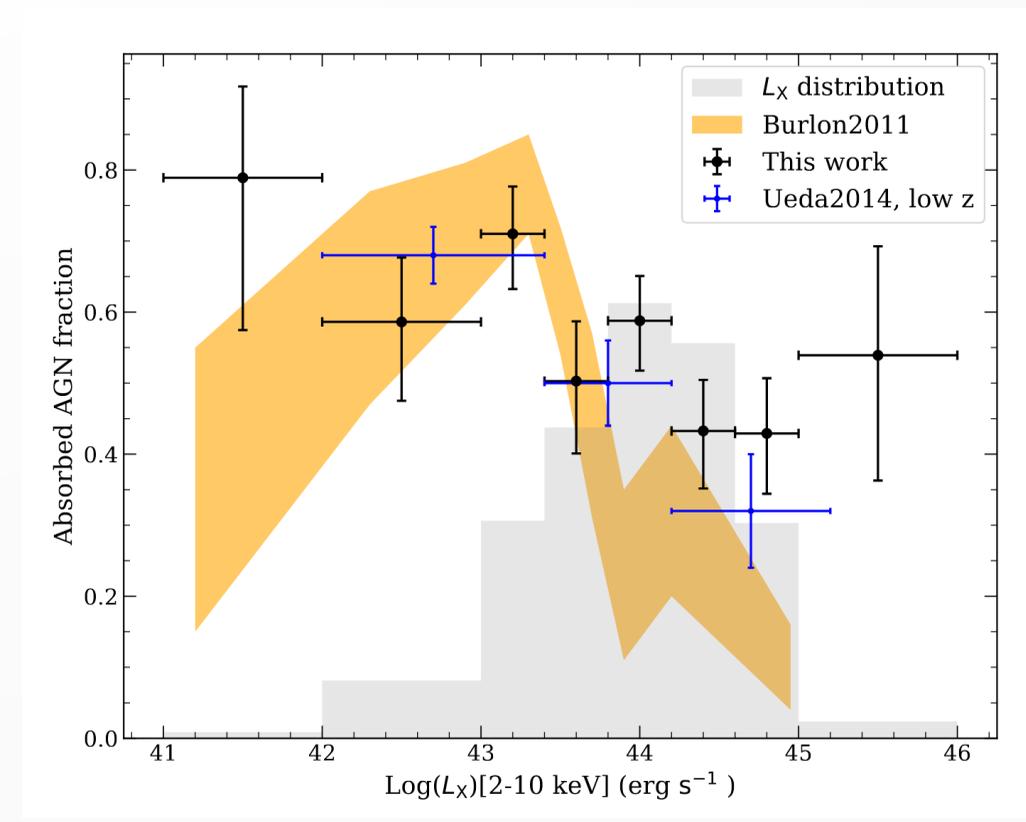
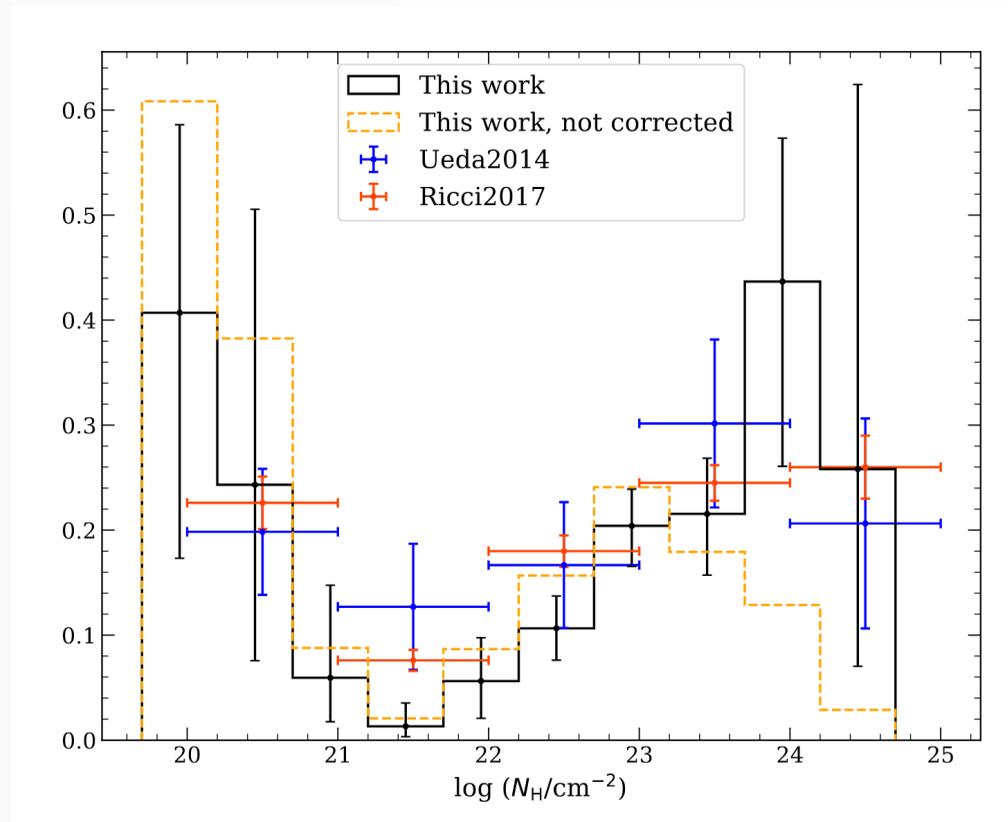
- We introduce *pyproffit* and *hydromass*, two public Python packages to reconstruct galaxy cluster properties
- The tools use multiscale decomposition to deproject and deconvolve observed profiles: King functions (density) and Gaussian processes (temperature)
- 1D PSF convolution with a mixing matrix is accurate at the sub-percent level
- $S_X$ ,  $T_{\text{spec}}$  and  $y_{\text{SZ}}$  profiles can be fitted jointly to reconstruct  $n_{3D}$ ,  $T_{3D}$
- The packages include fast Bayesian optimization using Hamiltonian Monte Carlo
- Within a single common framework *hydromass* also includes fitting with many popular mass models (e.g. NFW, Einasto), parametric forward model, and polytropic reconstruction
- Tests using mock data show that the method is accurate at the <3% level
- Extensive documentation is already in place for *pyproffit* and will be there soon for *hydromass*. Please try them out and give us feedback!

# Work in progress

- Joint fit with weak lensing data
- Add non-thermal pressure modeling
- Constrain line-of-sight elongation and 3D structure
- Marginalize over the position of the center
- Test reconstruction with mock observations of hydrodynamical simulations

# Bonus: AGN spectral parameters

- We recently presented a Bayesian approach to the reconstruction of AGN spectral parameters from X-ray survey data



*Ge et al. 2022 a,b*

ArXiv: 2111.14925 and 2111.15235

# Choice of parameters

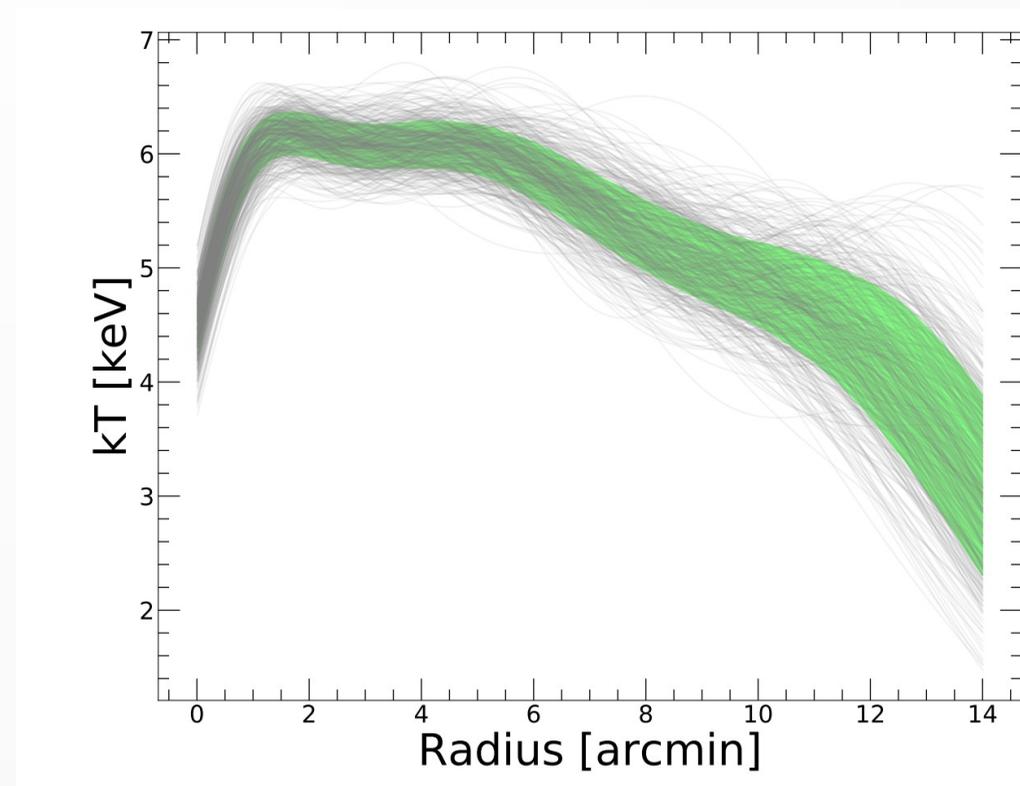
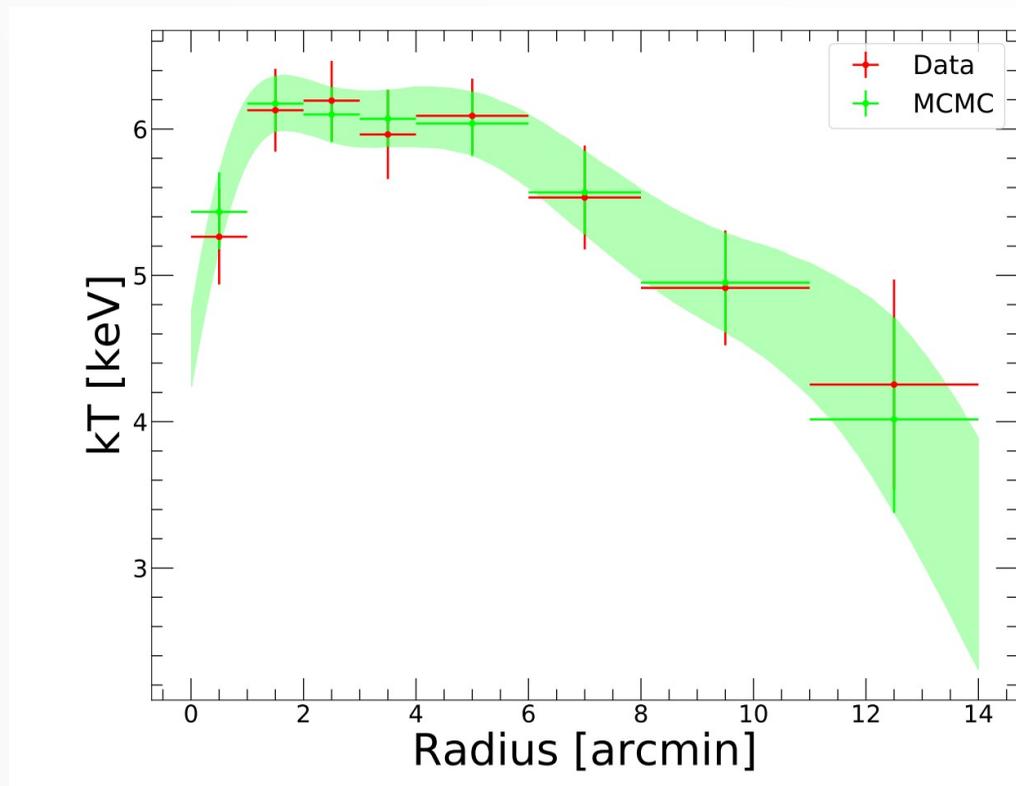
- Given a temperature profile with  $N$  points measured at radii  $\{r_i\}$ , we set  $P=100$  Gaussians with means logarithmically spaced between the center and the

$$\log \mu_j = \log r_0 + j(\log r_{max} - \log r_0)$$

- And standard deviations set to the bin size in order to kill fluctuations on a scale smaller than the binning
- The values of  $\{\sigma_j\}$  can be tuned to achieve more/less smoothing

# Implementation on 2D profiles

- First I started by testing how well the model can reproduce the shape of 2D profiles
- Optimization performed using PyMC3 (Hamiltonian Monte Carlo)



# Now let's move to 3D

- We set  $V_{i,j}$  the volume of (spherical) shell  $j$  projected onto (cylindrical) shell  $i$ , then the 2D temperature is given by

$$T_{2D}(r_i) = \frac{\sum_{j=1}^N V_{i,j} w_j T_{3D}(r_j)}{\sum_{j=1}^N V_{i,j} w_j}$$

with  $w_j$  the spectroscopic-like weights. Here we use Mazzotta et al. (2004) weights,

$$w_j = EM_{3D}(r_j) T_{3D}(r_j)^{-3/4}$$

- It is easy to substitute here another function for the weights and to include the PSF matrix, since only the relation between  $T_{2D}$  and  $T_{3D}$  is changed; otherwise the problem is the same